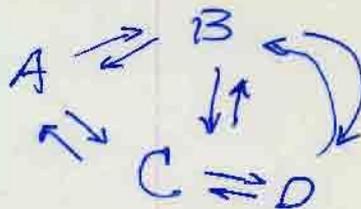


07:34-2

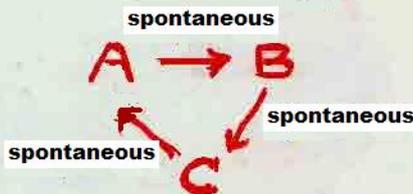
MICROSCOPIC REVERSIBILITY

MUST ACCOUNT FOR
 REVERSE OF ALL
 PROPOSED PROCESSES



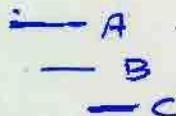
AT EQUILIBRIUM: FORWARD RATE = BACKWARD RATE
 FOR ANY PAIR

NEVER



Perpetual
 Motion!

implies that $G_A > G_B > G_C > G_A$



But $\Delta G = 0$ for cyclic process.



IF BOTH ARE 1st order:

AT EQUIL: $k[C] = k'[A]$

Forward rate = $k[C]$
 Back rate = $k'[A]$
 $K_{eq} = \frac{[A]}{[C]}_{eq} = \frac{k}{k'}$

ENZYME KINETICS

Michaelis-Menten - Briggs-Haldane model

$$\begin{array}{ccccccc}
 E & + & S & \xrightleftharpoons[k_{-1}]{k_1} & ES & \xrightleftharpoons[k_{-2}]{k_2} & EP & \xrightleftharpoons[k_{-3}]{k_3} & E + P \\
 \uparrow & & \uparrow & & \uparrow & & & & \\
 \text{Enzyme} & & \text{Substrate} & & \text{Complex} & & & &
 \end{array}$$

ignore (no back reaction)

EXPERIMENT:

$\text{rate} = k_2 [ES] \Rightarrow k_2 [E]_{\text{Total}}$
 $\text{rate} = k_1 [E][S] \times \frac{k_2}{k_2 + k_{-1}}$
 $[E]_{\text{Total}} = [E] + [ES] = E_0$

Assuming $[ES] = \text{Constant}$ (steady state)

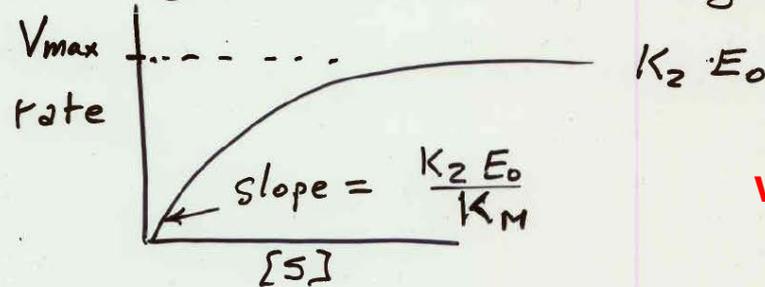
$$\text{rate} = \frac{k_2 E_0 [S]}{[S] + K_M} = \frac{k_1 E_0 [S] k_2}{k_1 [S] + (k_{-1} + k_2)}$$

$K_M = \text{Michaelis Constant} = \frac{k_{-1} + k_2}{k_1}$

What are the units of K_M ? Concentration = mol/L

LINE WEAVER - BURKE :

Plotting rate vs. $[S]$ gives



when $[S]$ very LARGE

when $[S]$ very small

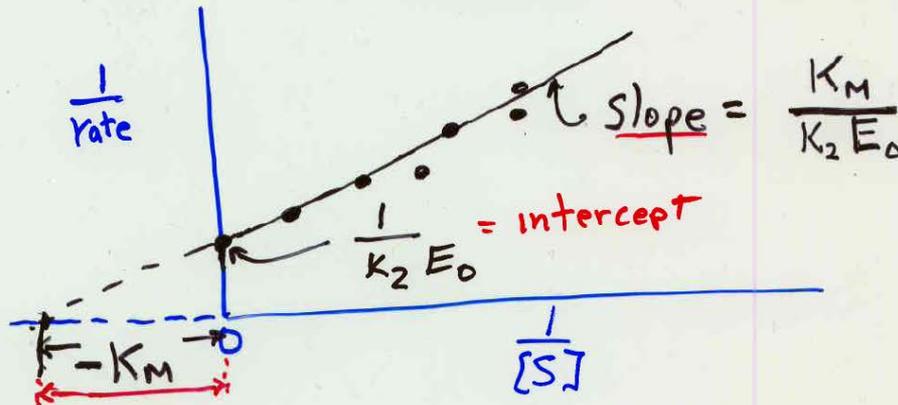
HARD TO EXTRACT K_M & k_2

$$\text{rate (initial)} = \frac{k_2 E_0 [S]}{[S] + K_M}$$

$[S]$ cancels if very LARGE

$$\frac{1}{\text{rate}} = \frac{[S] + K_M}{k_2 E_0 [S]} = \frac{1}{k_2 E_0} + \frac{K_M}{k_2 E_0 [S]}$$

equation of straight line



"CATALYTIC EFFICIENCY" * $\frac{k_2}{K_M}$ ENZYME EFFICIENCY

$$\text{rate} = \frac{k_2[S]E_0}{[S] + K_M} = \underbrace{\left(\frac{k_1[S]E_0}{k_1[S] + (k_{-1} + k_2)}\right)}_{\text{ENCOUNTER RATE}} \cdot \underbrace{\left(\frac{k_2}{k_1[S] + (k_{-1} + k_2)}\right)}_{\text{Fraction of success}}$$

[S] is negligible at low [S]

$$K_M = \frac{k_{-1} + k_2}{k_1}$$

$$\Rightarrow \left(\frac{k_2}{K_M}\right) [S] [E_0] \leftarrow \text{2nd order rate constant}$$

How large can k_2/K_M be?

A small K_M is like a small dissociation constant

Substrate	$k_2 \text{ s}^{-1}$	$K_M \text{ (M)}$	$\left(\frac{k_2}{K_M}\right)^*$
<u>Catalase</u>	4×10^7	1.1	4×10^7
<u>Fumarase</u>	800	5×10^{-6}	1.6×10^8

*Specificity Constant in our text

$$K_M = \frac{k_{-1} + k_2}{k_1} = \frac{k_{-1}}{k_1} + \frac{k_2}{k_1} = K_d + \frac{k_2}{k_1}$$

ES $\xrightleftharpoons[k_1]{k_{-1}}$ E + S dissociation constant of E·S

Is k_2 ever $\gg k_1$???

$\frac{k_2}{K_M}$ can never be $> \sim 10^9 \text{ M}^{-1} \text{ s}^{-1}$
diffusion limit

Single Molecule Kinetics

This shows that a single enzyme shows an efficiency that varies in time, yet the average is the same as for a typical macroscopic solution.

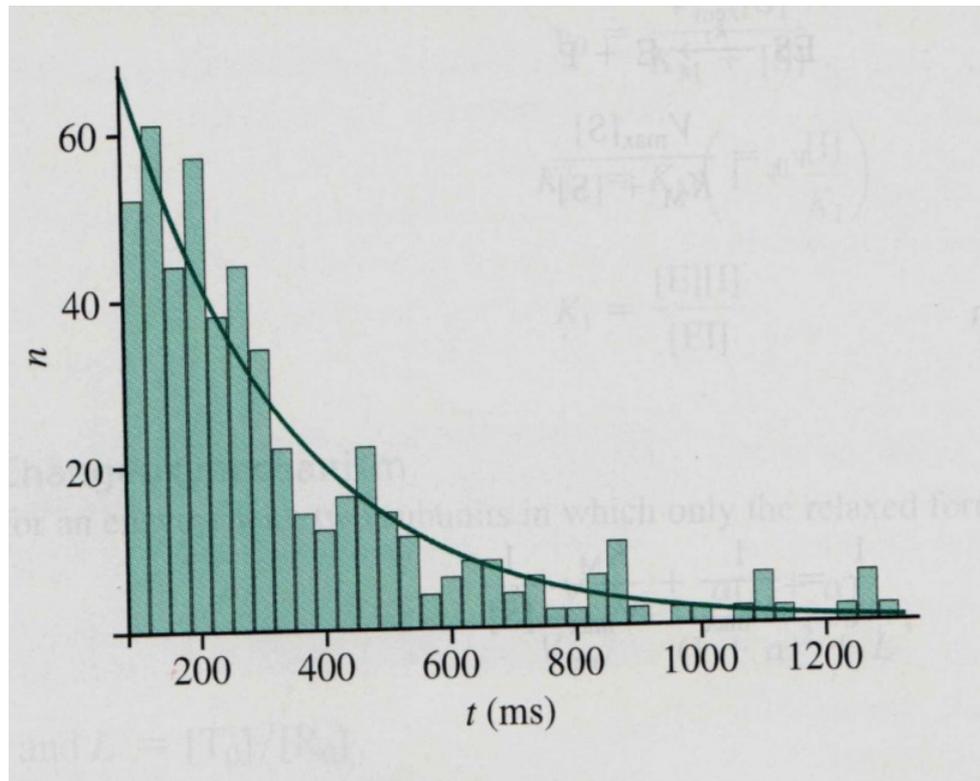


FIGURE 10.8 Plot of the occurrence of different lifetimes for a single molecule of the enzyme substrate complex, E·FAD·S, of the enzyme cholesterol oxidase. The substrate S is cholesterol. The single molecule is monitored by its fluorescence when FAD is in its oxidized form; when FAD is reduced to FADH₂ there is no fluorescence. The exponential distribution of lifetimes gives a value for the rate coefficient for formation of product $k_2 = 3.8 \text{ s}^{-1}$.

Arieh Warshel, stated the truth about enzyme action in 1976:

“The energy provided by protein folding reduces the activation energy by preorganizing the active site to provide large electrostatic stabilization of the transition state(s).”

(paraphrased)

He has preached this since 1976 and has been awarded the Nobel prize along with his mentors for associated development of modeling methods, and yet this idea still is not well accepted.

ELECTROSTATICS

Potential Energy

Coulomb's Law =

$$U_{12} = \frac{q_1 q_2}{4\pi\epsilon_0 r_{12}} = \text{electrostatic potential energy in Joules}$$

← charges in Coulombs
 ↗ distance apart in meters

$$\frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9$$

For 2 elementary charges separated by 1 Å:

$$U = \frac{(9.0 \times 10^9) (1.6 \times 10^{-19})^2}{1 \times 10^{-10}} = \underline{\underline{23 \times 10^{-19} \text{ J}}}$$

Per mole: $23 \times 10^{-19} \times 6 \times 10^{23} = 1,380,000$

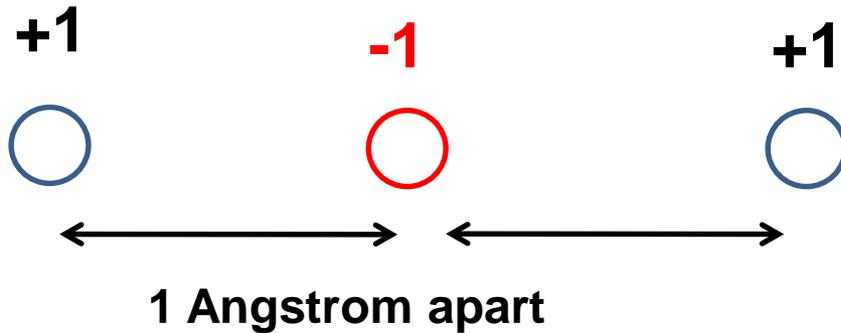
$$= \boxed{1389 \text{ kJ/mol}}$$

or -1389 kJ/mol if opposite charges:
 ⊕.....⊖

YOUR Coulomb's Law = 1389 kJ/mol times the sum over all pairs i,j
 where z_i = charge in units of e, and r_{ij} is in Å

$$\frac{(z_i)(z_j)}{r_{ij}}$$

What about a collection of point charges?



Are charges 1 and 3
“shielded” by 2????

There really is no such thing
as shielding in Coulomb’s Law

$$\text{Potential Energy} = 1389 \text{ kJ/mol} \left[\frac{(z_1)(z_2)}{r_{12}} + \frac{(z_1)(z_3)}{r_{13}} + \frac{(z_2)(z_3)}{r_{23}} \right]$$

$$\text{Potential Energy} = 1389 \text{ kJ/mol} \left[\frac{-1 \times 1}{1} + \frac{1 \times 1}{2} + \frac{-1 \times 1}{1} \right]$$

$$= 1389 \text{ kJ/mol} [-1 + 0.5 - 1] = 1389 \text{ kJ/mol} [-1.5] = -2084 \text{ kJ/mol}$$

This is the **only potential energy** that is in Quantum Mechanics: the Schrodinger Equation for atoms and molecules! (i.e., **CHEMISTRY**)

This is therefore what determines all **molecular** energies when determined by **quantum mechanics**.

The sum is **ALWAYS negative** for a **stable** atom or molecule.

How much is an equilibrium constant or a rate constant changed by a seemingly small electrostatic interaction ??

$$\text{Equilibrium constant } K = 10^{\frac{-\Delta G^0}{2.3RT}} = 10^{\frac{-\Delta G^0}{5.7 \text{ kJ}}}$$

$$\text{Rate constant } k = A e^{\frac{-E_a}{RT}} = A 10^{\frac{-E_a}{5.7 \text{ kJ}}}$$

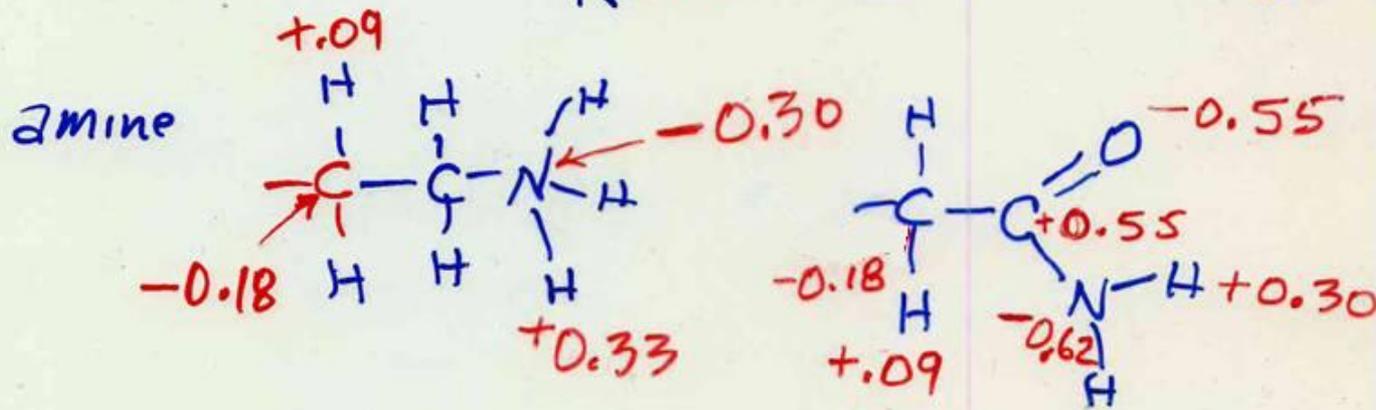
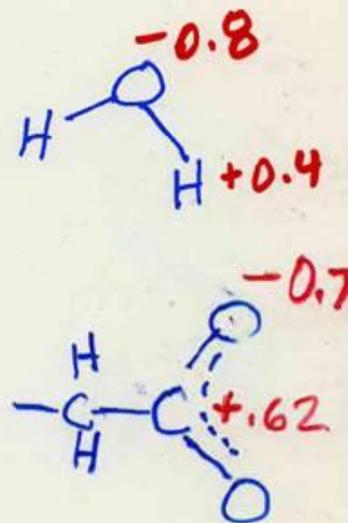
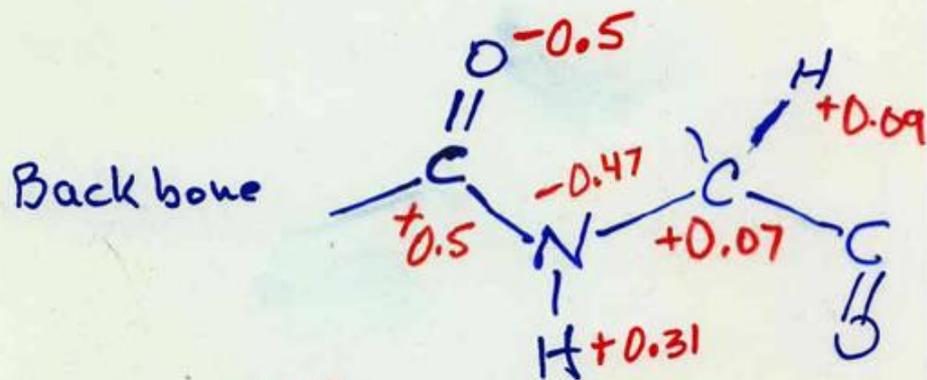
Consider a +1 and a -1 charge 100 Angstroms apart

$$U = 1389 \times (1)(-1) / 100 = -13.9 \text{ kJ/mol}$$

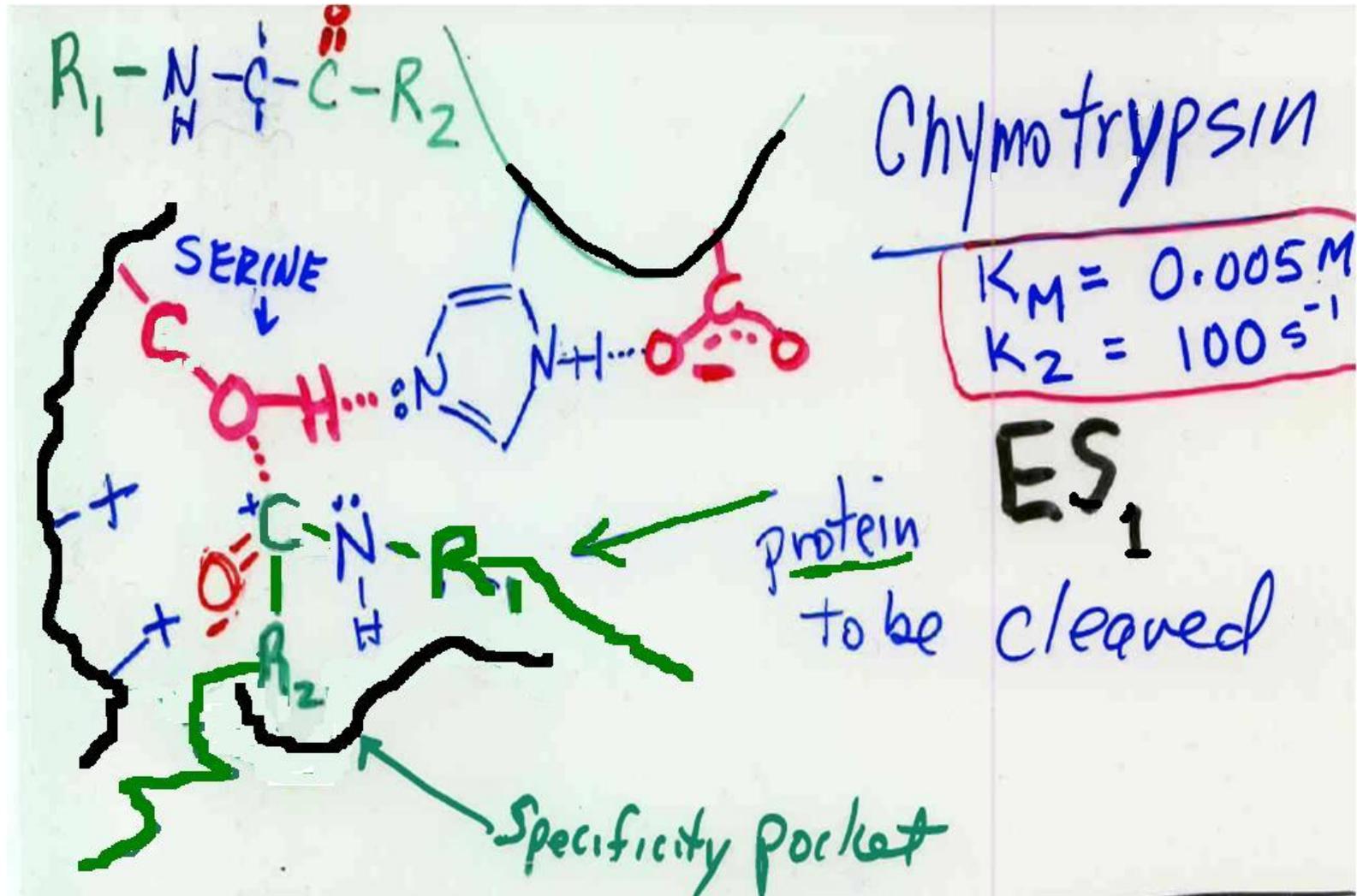
$$10^{\frac{13.9}{5.7}} = 10^{2.4} = 250 \text{ i.e., 250 times larger } K!$$

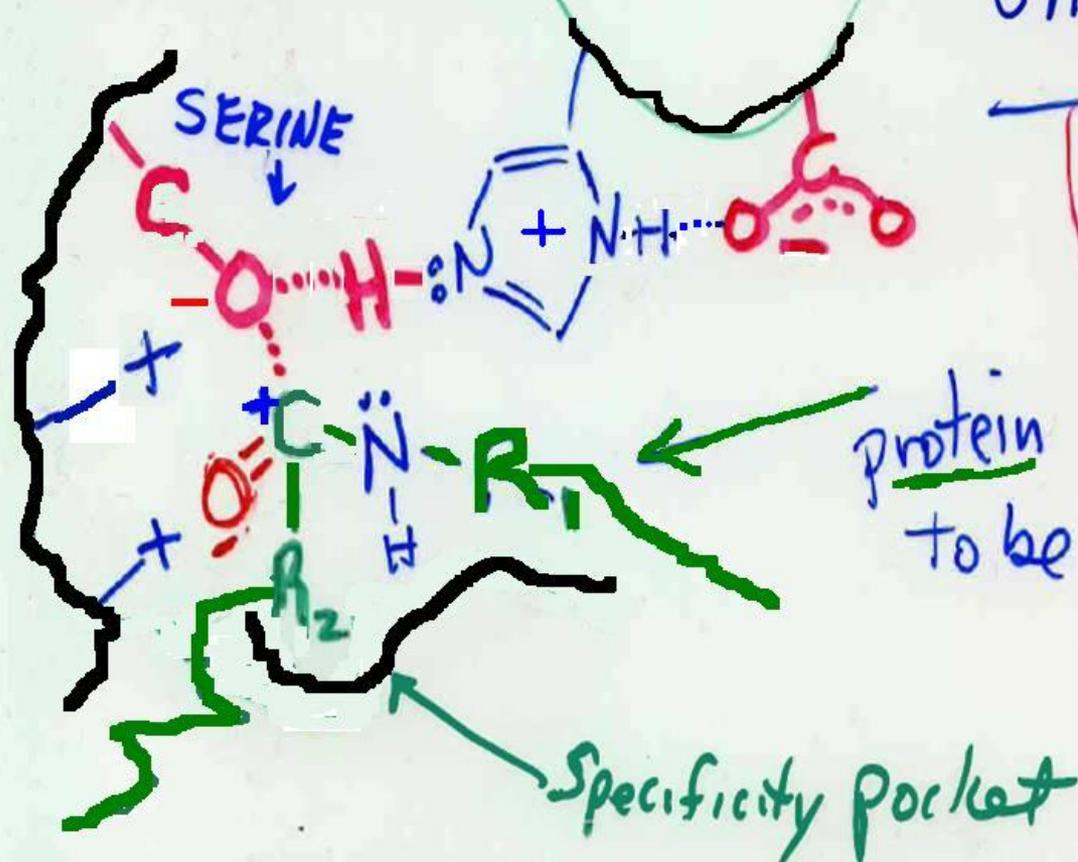
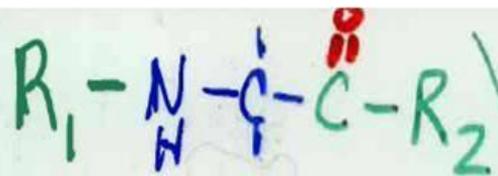
Atoms are treated as point charges and point masses.

Some typical values:



Example of electrostatic importance in an enzyme



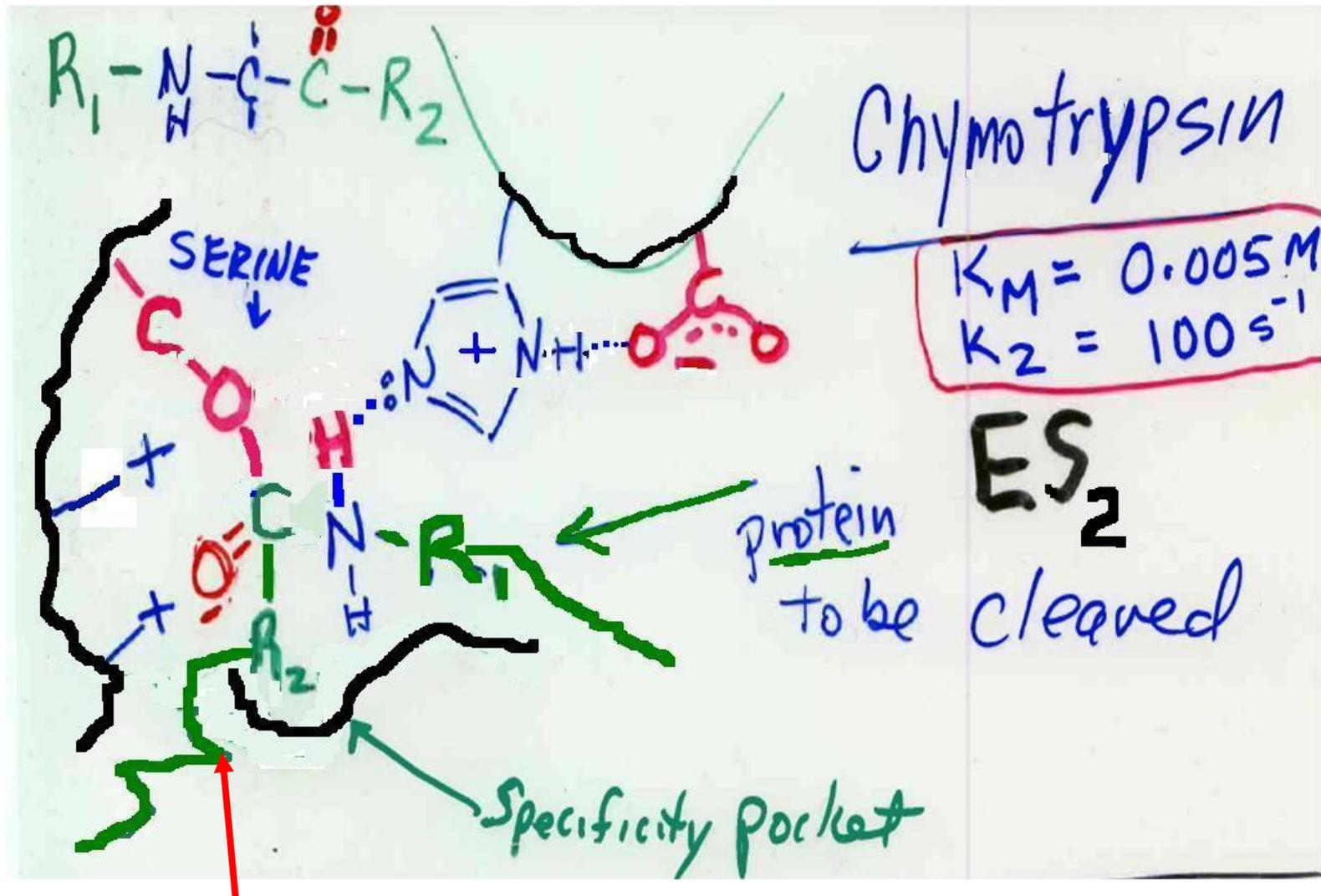


Chymotrypsin

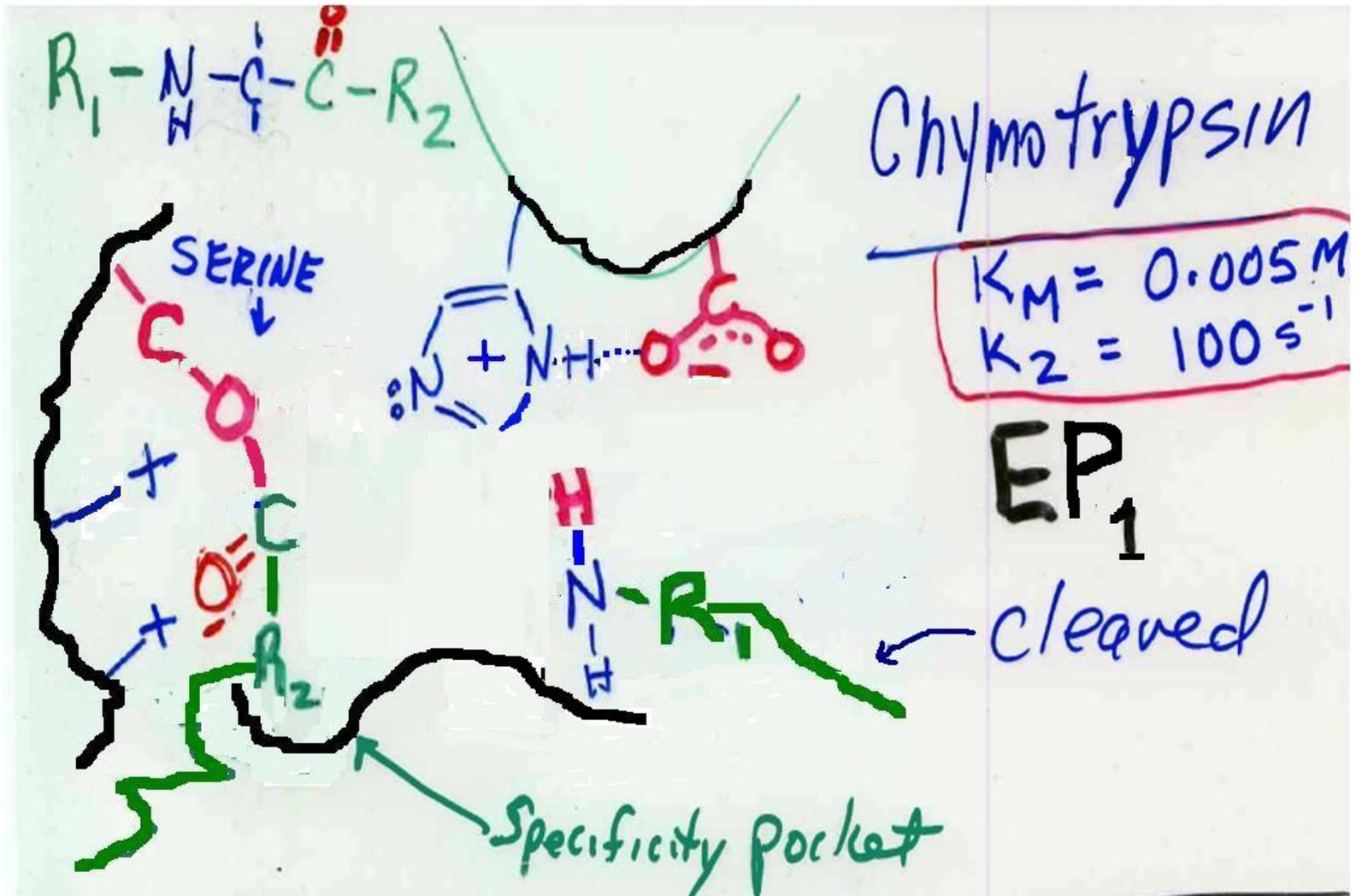
$$K_M = 0.005 \text{ M}$$

$$K_2 = 100 \text{ s}^{-1}$$

ES_1
cleaved

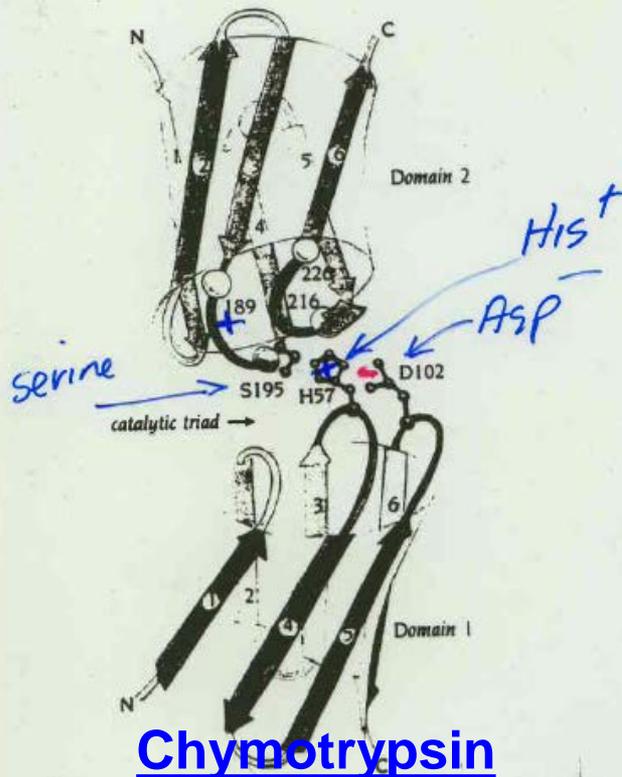


This part of substrate is now covalently attached to the enzyme



“Convergent Evolution”

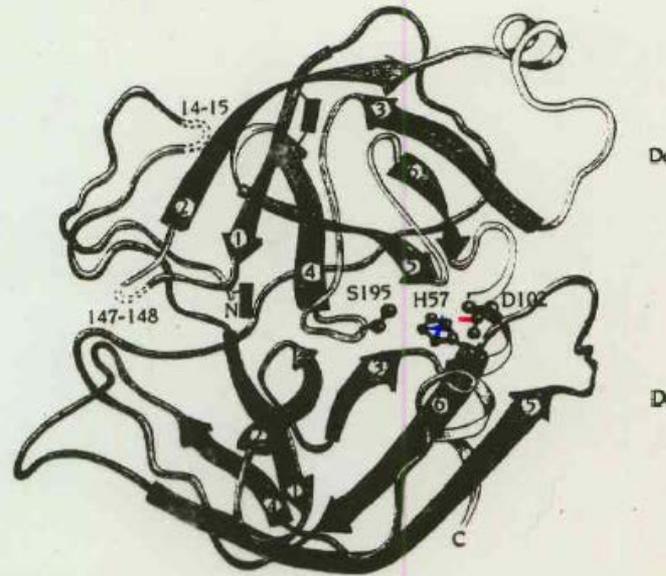
Subtilisin (bacterial)



Chymotrypsin

- oxygen hole (res. 193-195)
- main-chain substrate binding (res. 214-216)
- substrate specificity pocket (res. 189, 216, 226)

Figure 15.10 Topological diagram of the two domains of chymotrypsin, illustrating that the essential active-site residues are part of the same two loop regions (3-4 and 5-6) of the two domains (colored red). These residues form the catalytic triad (red), the oxyanion hole (green), and the substrate binding regions (yellow and blue) including essential residues in the



Convergent evolution has produced two different serine proteinases with similar catalytic mechanisms

These four features all occur in an almost identical fashion in all members of the serine proteinase superfamily of homologous enzymes, which includes other enzymes chymotrypsin, trypsin, elastase, and thrombin. Naively one might imagine that such a combination of four characteristic features had arisen only once during evolution to give an ancestral molecule from which all serine proteinases diverged. However, subtilisin, a bacterial serine proteinase with a different amino acid sequence, and as we will see, a three-dimensional structure very different from the mammalian serine proteinases, exhibits these same four characteristic features. Subtilisin is not evolutionarily related to the chymotrypsin family of enzymes; nevertheless, the atoms in subtilisin that participate in the catalytic triad, in the oxyanion hole, and in substrate binding are in a