

REVIEW: First Law in simple words and the main equation:**Energy of the system + surroundings is conserved.**

$$\Delta U = q + w \quad (\text{eq. 2.26, p. 24})$$

$$\Delta U =$$

Energy change
of system
during process

$$q +$$

Energy absorbed by
system because of a
temperature difference
between system and
surroundings.

Something in the
SURROUNDINGS
must get colder or
hotter,

or else $q = 0$

DISordered energy

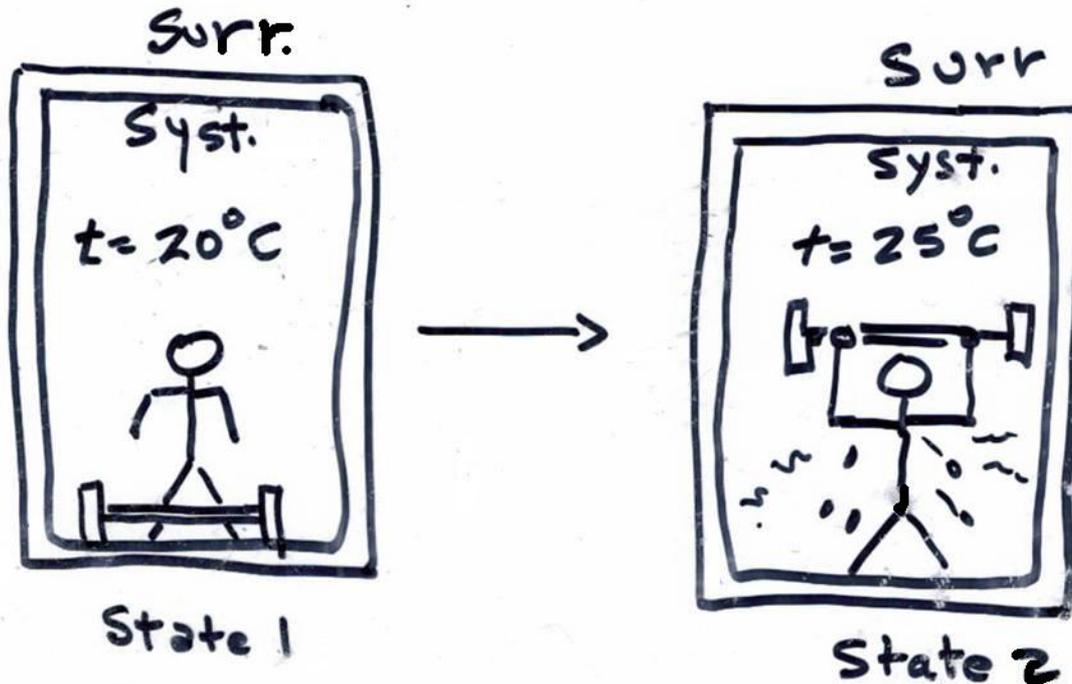
$$w +$$

Energy absorbed by
system because of a
force acting
*between system and
surroundings.*

Something in the
SURROUNDINGS
must move against
force (or the
equivalent),
or else $w = 0$

ordered energy

Isolated System = Thermally insulated & No mechanical connection to surroundings



Weight lifter works out and the room heats up from 20°C to 25°C

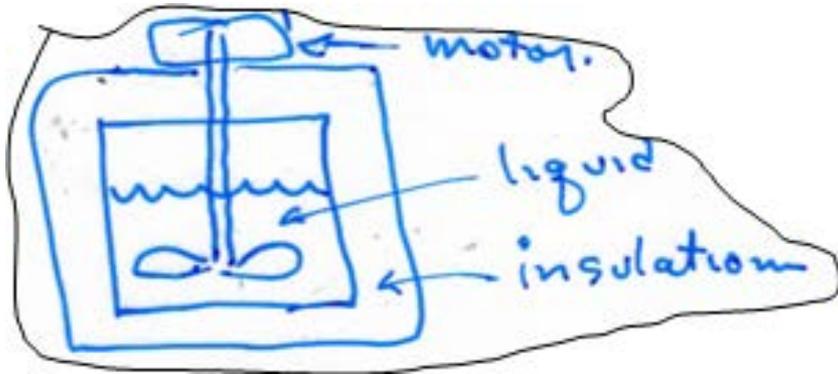
Are ΔU , q , w positive, zero, or negative?

Answers: ΔU , q , w all = ZERO because nothing is happening in the surroundings

Two More Examples:

T of water (the system) is increased 10°C by two different paths:

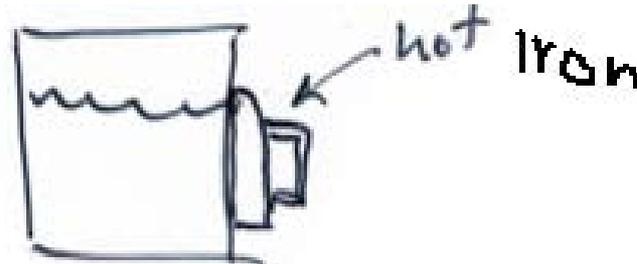
- 1) by friction from stirring by a motor from surroundings while thermally insulated from the motor. **What are q and w?**



$$q = 0 \text{ (insulated)}$$
$$w = + \text{ (motor does work on water)}$$

$$\Delta U = q + w \text{ (Eq. 2.26, page 24)}$$

$$\Delta U = w$$



- 2) by a hot iron in thermal contact with the system.

What are q and w?

$$q = + \text{ because temperature of iron decreased; } w=0; \Delta U = q$$

Lesson: q and w depend on path, but ΔU is **independent of path** because initial and final states of system are same in both cases.

In old chemistry books and in most engineering texts one sees:

$$\Delta U = q - w$$

Is this wrong?

What is the definition of w in this case?

w is defined as work obtained **FROM** the system
if we use the above equation

Relevance of $\Delta U = q + w$

If we choose to make a bonfire of our food

$\Delta U = q_{\text{max out}}$ and useful $w = 0$

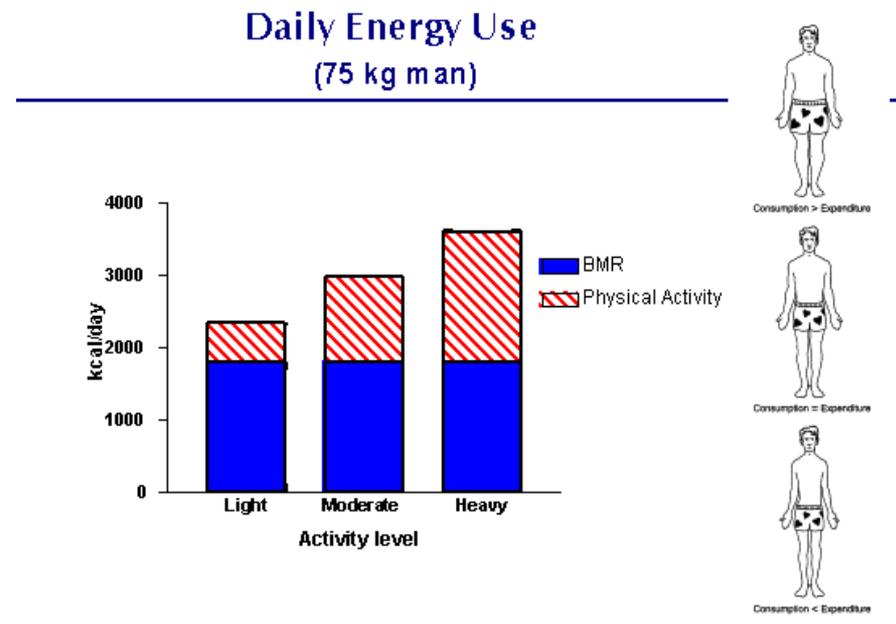
If we choose to eat our food, the same reaction: food + Oxygen \rightarrow CO₂ + H₂O

$\Delta U = q_{\text{min out}} + W_{\text{max out}}$

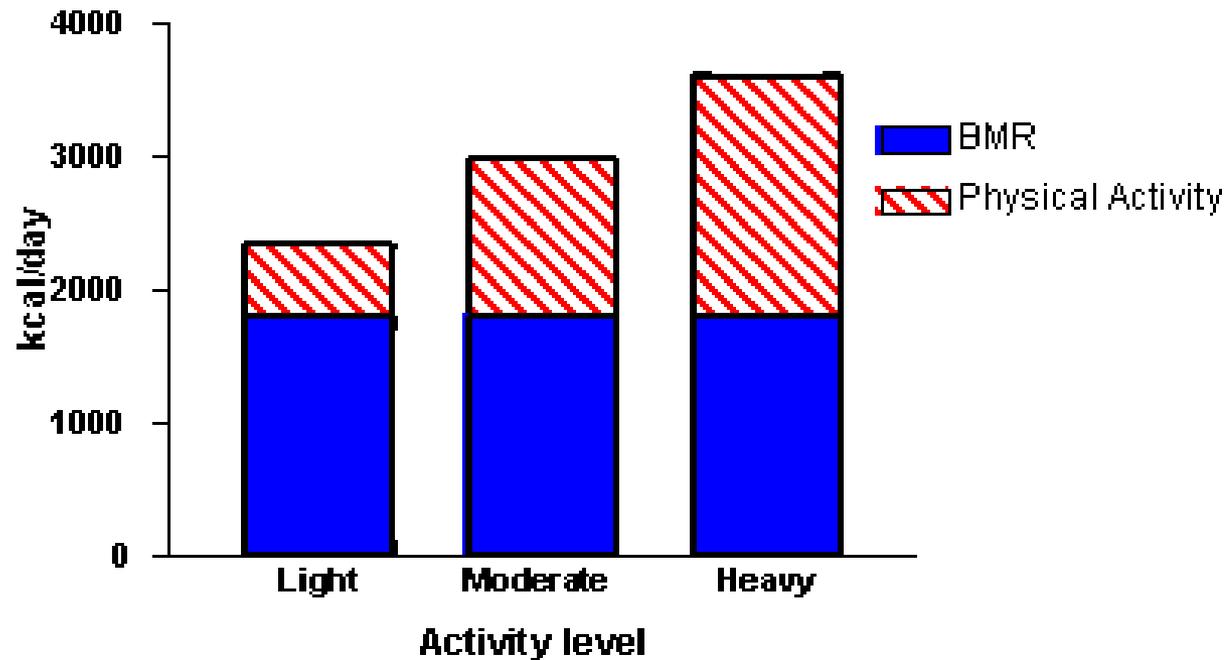
What work is being done with the 2000 kcal/day we require doing nothing?

Living things are able to get the maximum work from food. But typically not all of the energy can be turned to work.

(BMR = basic metabolic rate)



Daily Energy Use (75 kg man)



Consumption > Expenditure



Consumption = Expenditure



Consumption < Expenditure

Etter/Marks, Marks og Smith

(BMR = basic metabolic rate)

Living things have evolved to get the most possible work from the ΔU from burning food.

ATP (adenosine triphosphate) is the major currency of work in our cells;

ATP is continually used and rebuilt throughout the day.

Amazingly, if you add up the amount of ATP that is built each day, it would roughly equal the weight of your entire body.

This ATP is spent in many ways: to power muscles, to make sure that enzymes perform the proper reactions, to PUMP IONS, +100,000 other...

but roughly a third of the ATP made by our cells is spent to power the sodium-potassium pump (a PROTEIN).

Life requires **cells** to have high K⁺ concentration, but **blood** has high Na⁺

[Sodium-Potassium Pump Cartoon](#)

Calculating Work

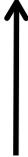
work = w = external force x distance

(if the force is constant)

between
the system and
SURROUNDINGS



displacement
in the **SYSTEM**



The sign (+ or -) depends on whether system expands or contracts in response to the force.

What if the force is NOT constant? Calculus

a very small amount of work = $dw = f_{ext}(x)dx$

where dw, dx mean infinitesimally small (but we can think of this as just meaning really, really, really, small);

$f_{ext}(x)$ means the force is NOT CONSTANT, but is a “function of x ”, i.e., depends on x

Now just add up all the small bits:

$$W = \int_{x_1}^{x_2} f_{ext}(x)dx$$

Note that the integral sign is an S, standing for SUM

Constant Force Case:

$$W = f_{ext} \int_{x_1}^{x_2} dx = f_{ext}(x_2 - x_1) = f_{ext}\Delta x$$

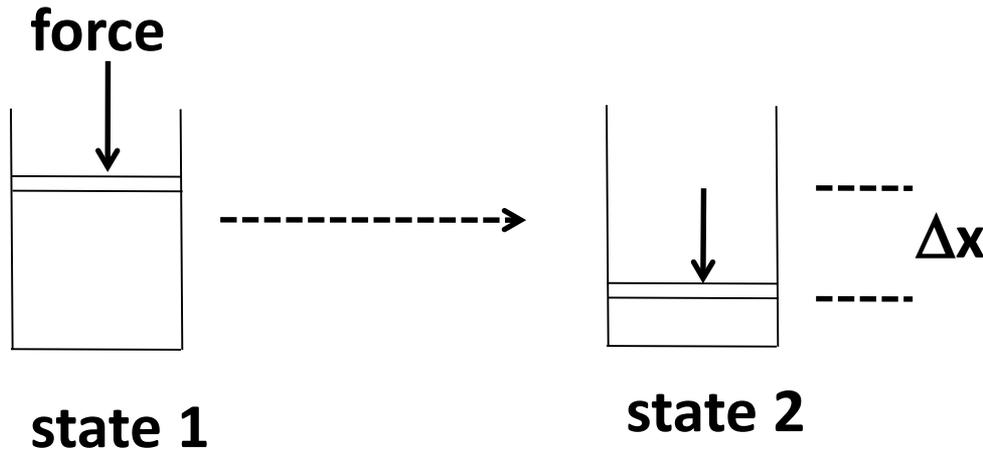
Earth's gravity is a nearly constant force.

force = mass x acceleration = mg, where $g = 9.8 \text{ ms}^{-2}$ at the earth's surface

- If you hold 1 kg (2.2 lbs) you feel a force = $1 \text{ kg} \times 9.8 \text{ ms}^{-2}$
= $9.8 \text{ kg m s}^{-2} = 9.8 \text{ Newtons} = \mathbf{9.8 \text{ N}}$
- Work to raise this 1 meter = $9.8 \text{ kg m s}^{-2} \times 1 \text{ m} = 9.8 \text{ kgm}^2\text{s}^{-2}$
= **9.8 Joule = 9.8 J**
- Work for you to climb a 1000 m mountain (3300 ft) like Baldy:
= $100 \text{ kg} \times 9.8 \text{ ms}^{-2} \times 1000 \text{ m} \approx 100 \times 10 \times 1000 = \approx 10^6 \text{ J} = \mathbf{10^3 \text{ kJ}}$
dividing by 4.184 kJ per kcal gives: **250 kcal = ~2.5 slices of bread.**
Doing “nothing”, your body requires ~2000 kcal/day.
that is the equivalent of climbing 10,000* m, or 20 slices of bread!
*** Climbing Mt. Everest starting at sea level**

Expansion/Compression of System with **Constant** External Pressure

consider a **cylinder** filled with gas and capped with a piston



$$work = w = f_{ext} \Delta x$$

multiply top and bottom by Area of cylinder = A

$$w = \frac{f_{ext}}{A} A \Delta x = \text{pressure} \times \text{volume} = P_{ext} \Delta V$$

but, what is the sign of w??

What is the sign??? ΔV is obviously negative and pressure is positive, but work is done *on* the system. Therefore, w is positive. The correct equation for this kind of work is : $w_{pv} = -p_{ext}\Delta V$

ALWAYS TRUE, for constant external pressure.

SI unit of Pressure $1 \text{ Nm}^{-2} = 1 \text{ Pascal} = 1 \text{ Pa}$

Note: $1 \text{ Nm m}^{-3} = 1 \text{ Jm}^{-3} = 1 \text{ Pa}$ also

$1 \text{ bar} = 1 \times 10^5 \text{ Pa}$ (the usual modern standard state)

$1 \text{ atm} = 1.013 \times 10^5 \text{ Pa}$

$1 \text{ liter} = 1 \text{ L} = 1 \times 10^{-3} \text{ m}^3$ so:

$1 \text{ L atm} = 10^{-3} \text{ m}^3 \times 1.013 \times 10^5 \text{ J m}^{-3} = 101.3 \text{ J}$

$1 \text{ L bar} = 10^{-3} \text{ m}^3 \times 1.000 \times 10^5 \text{ J m}^{-3} = 100 \text{ J}$ 

Other common units of pressure

1 atm = 14.7 lbs/square inch

1 atm = **760 mm of mercury** = 760 torr = 29.9 inches Hg

This comes from the density of Hg, 13.6 g/cm³

or 13.6 x 10³ kg/m³

and **pressure = acceleration of gravity x density x height**

$$9.8 \text{ ms}^{-2} \times 13.6 \times 10^3 \text{ kg m}^{-3} \times 0.76 \text{ m} = 1.013 \times 10^5 \text{ kg m}^{-1} \text{ s}^{-2}$$

$$= 1.013 \times 10^5 (\text{kg m s}^{-2})\text{m}^{-2} = 1.013 \times 10^5 \text{ Pa} = 1 \text{ atm}$$